

# Physics 1C Sample Tests

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## Physics 1C Test 1

# and Problems

### 1. BALANCE

You wish to use gravity and electrostatic fields to trap an electron. As a first step in your calculations how many coulombs should you put on a point .016 m below the electron to just cancel out gravity?  $q$  electron =  $1.6 \times 10^{-19}$  coulombs,  $m$  electron =  $9.11 \times 10^{-31}$  kg,  $k = 9 \times 10^9$  n m square/cb squared

$$9.11 \times 10^{-31} \times 9.8 \times .016 \times .016 / 9 \times 10^9 / 1.6 \times 10^{-19}$$

- A.  $6.29 \times 10^{23}$ , B.  $5.19 \times 10^{-24}$ , C.  $1.59 \times 10^{-21}$ ,  
D.  $(1.59 \times 10^{-24})$ , E.  $7.95 \times 10^{-25}$

### 2. LINE CHARGE

Find the electric field at the origin due to a line of charge along the x axis from  $x = 4.7$  m to  $x = 10$  m. The charge density is  $1.1 \times 10^{-10}$  cb/m.

$$-9 \times 10^9 \times 1.1 \times 10^{-10} \times (1/4.7 - 1/10)$$

- A. .0396, B. .0755, C. (.112), D. .166, E. .44

### 3. G TO C

Show how Coulomb's Law follows from Gauss' Law. Explain carefully.

### 4. SPHERE CHARGE

Find the electric field 2.5 m from the center of a region of space with a charge density given by  $\rho = 5.5 \times 10^{-15} r^{2.3}$ .

$$5.5 \times 10^{-15} \times 2.5^{2.3+1} / (8.85 \times 10^{-12} \times (2.3+3))$$

- A. .000605, B. .0013, C. .00182, D. (.00241), E. .00828

### 5. E FROM PLANE

Show that the electric field produced by an infinite conducting plane is given by  $\sigma / \epsilon_0$  where  $\sigma$  is the charge per unit area. Explain VERY carefully.

### 6. CAVITY

A spherical region carries a uniform charge per unit volume  $\rho_0$ . Let  $r$  be the vector from the center of the sphere to a point P within the sphere. (a) Show that the electric field at P is given by  $E = \rho_0 \times r$

( $\times \epsilon_0$ ). (b) A spherical cavity is created in the above sphere. Show that the electric field at all points within the cavity is  $E = \rho_0 \times a / (3 \times \epsilon_0)$ , where  $a$  is the vector connecting the center of the sphere with the center of the cavity.

## Physics 1C Test 2

## 1. LINE POTENTIAL

Find the potential due to a charged line of charge density  $\lambda$ . The point of interest is on the axis of the line, and a distance  $a$  from the near end of the line. The line is of length  $b$ . The potential is:  $k \lambda \ln((a+b)/a)$

## 2. V VS R

Show that for two spheres connected by a conductor the ratio of the fields at the surfaces is given by  $E/e = r/R$  where one sphere has a radius  $R$  and field  $E$  and the other sphere has a radius  $r$  and field  $e$ .

## 3. SPHERE APPROXIMATION

Find the capacitance of two concentric spheres separated by a distance,  $d$ , small compared to their radius. Show that the capacitance is approximately the same as the capacitance of two parallel plates with the same area and separation:  $C = A/d$ . Use only  $C = q/V$ , Gauss' Law, and  $dV = E dx$ .

$$C = A\epsilon_0/d$$

## 4. SHUFFLE C

Two capacitors ( $7.1 \times 10^{-6}$  farads and  $.000036$  farads) are connected in series and 10 volts is applied to the pair. The voltage is removed and the capacitors are connected in parallel, plus to plus. What is the new voltage?

$$20 \times 7.1 \times 10^{-6} \times .000036 / (7.1 \times 10^{-6} + .000036) \times 2$$

A. 1.37, B. 1.67, C. (2.75), D. 4.93, E. 7.61

## 5. PARALLEL

Derive the equivalent resistance of two resistors connected in parallel.

## 6. R V CIRCUIT

A circuit has three parts, in series. Part 1 is a 130 volt battery, 12 ohms internal resistance. Part 2 is two resistors in parallel, 120 and 200 ohms. Part 3 has a 76 ohm resistor in parallel with a 36 volt battery, reversed, 25 ohms internal resistance. How many amps of current flow through the 130 volt battery? Consider the plus direction to be the direction the 130 volt battery pushes current.

$$(130 - 36 \times 76 / (76 + 25)) / (12 + 120 \times 200 / (120 + 200) + 25 \times 76 / (76 + 25))$$

A. .448, B. .771, C. (.973), D. 1.07, E. 2.62

Physics 1C Test 3

1. RC DERIVATION

Show that the charge on a capacitor C connected in series with a resistor R is given by  $Q=Q(\text{initial}) \text{EXP}(-t/RC)$

2. CYCLETROTON

You plan to build a large, cheap cycletron using the Earth's magnetic fields ( $1 \text{ E } -4 \text{ T}$ ) and orbiting just above the Earth's atmosphere (radius  $5.9 \text{ E}6 \text{ m}$ ). What energy, in volts, should protons be given to just circle the earth?  $q=1.6 \text{ E } -19 \text{ clb}$ ,  $m = 1.67 \text{ E } -27 \text{ kg}$ .

$$1.6\text{E}-19 \cdot 1\text{E}-8 \cdot 5.9 \text{ E}6 \cdot 5.9 \text{ E}6 / 2 / 1.67\text{E}-27$$

- A. (1.67 E13), B. 1.93 E13, C. 3.26 E13, D. 5.35 E13, E. 7.1 E13

3. B FIELD OF LOOP

A circular loop of radius .15m is carrying a current of 11 amps. Find the magnetic field on the axis of the loop at a distance of .63 meters. Start from  $dB=\mu \cdot i \cdot dl \cdot r / (4 \cdot \pi \cdot r^{*3})$ .  $\mu=1.26 \text{ E}-6$

$$1.26\text{E}-6 \cdot 11 \cdot .15 \cdot .15 / (2 \cdot (.15 \cdot .15 + .63 \cdot .63) \cdot 1.5)$$

- A. (5.74 E-7), B. 9.91 E-7, C. 1.52 E-6, D. 1.68 E-6, E. 2.34 E-6

4. FLYING RING

Remember the demonstration with a magnetic coil connected to AC power and an aluminum ring. The ring was placed on top of the coil and, although aluminum is non magnetic, the ring was thrown to the ceiling. Explain 1. Why was there any force on the ring? 2. Why the ring went UP? Use clear diagrams and Faraday's Law.

5. LENS AND MIRROR, REAL

An object is 18 m to the left of a lens of 7.1 m focal length. A mirror of 13 m focal length is 110 m to the right of the lens. How far from the mirror is the image it forms?

$$13 / (1 - 13 / (110 - 7.1 \cdot 18 / (18 - 7.1)))$$

- A. 5.83, B. 8.25, C. 12.2, D. (15), E. 32.5

J CROSS B GENERATOR

An ionized gas (a plasma) has a temperature of 5,700 K. 11,000 K is about equal to level of energy (1 electron charge times 1 volt). The plasma flows down a channel of width .76 m with a velocity due to its energy ( $1/2 mv^2$ ). There is a magnetic field of 2.4 T perpendicular to the flow of the plasma. The  $v$  cross  $B$  force will push electrons toward the wall. This motion charges the wall and produces an electric field opposing the  $v$  cross  $B$  force. What is the equilibrium voltage when the forces are equal? electron mass =  $9.11 \times 10^{-31}$  kg, electron charge =  $1.6 \times 10^{-19}$  C.

$$.76 \times 2.4 \times \sqrt{(2 \times 5,700 \times 1.6 \times 10^{-19} / 9.11 \times 10^{-31} / 11000)}$$

- A. (778,000); B. 857,000, C.  $1.81 \times 10^6$ , D.  $2.32 \times 10^6$ , E.  $3.43 \times 10^6$

Physics 1C Test 4

1. INDUCTANCE TWO

Show that the inductance of two parallel wires (radius  $a$ , separation of centers  $d$ , length  $L$ ) carrying equal but opposite currents, is given by:

$$L = (\mu_0 / \pi) L \ln((d-a)/a)$$

OR

Use the energy density of a magnetic field  $B^2 / (2 \mu_0)$  to show that the self inductance of a length  $l$  of a long wire due to the magnetic flux inside the wire is  $(\mu_0 / 8 \pi) l$ . Assume the current distribution is uniform across the wire.

$$\mathcal{E} = -L (di/dt)$$

2. LC OSCILLATION

Find the inductance required to oscillate at  $1.3 \times 10^6$  Hz with a .0011 farad capacitor. Derive the equation needed starting from the definitions of capacitors, etc. or from the definitions of reactance.

$$1 / ((1.3 \times 10^6 \times \pi)^2 \times .0011)$$

- A.  $5.49 \times 10^{-12}$ , B.  $7.9 \times 10^{-12}$ , C.  $(1.36 \times 10^{-11})$ , D.  $1.5 \times 10^{-11}$ ,  
E.  $4.16 \times 10^{-11}$

3. PHASER

For an RC phaser diagram: Sketch and explain the diagram. Include the maximum and observed voltages. Use the diagram to find  $Z$  and  $\delta$  for the power supply voltage in  $V = (i_0 \sin(\omega t + \delta))$ .

4. LRC DRIVEN

A LRC circuit is driven by a source of 110 volts rms at 770 Hz. If  $L = .00088$  henries and  $C = .000025$  farads, what is the power delivered to a 9.2 ohm resistor?

$$9.2 \times 110 \times 110 / (9.2^2 + (\pi^2 \times 770^2 \times .00088^2 - 1 / (\pi^2 \times 770^2 \times .000025^2))^2)$$

- A. (1,110), B. 1,300, C. 2,910, D. 3,150, E. 4,610

5. WAVE EQUATION

Show that  $E = E(x - vt)$  solves the wave equation  $\nabla^2 E = (\mu_0 \epsilon_0) \partial^2 E / \partial t^2$ . Also show that  $v = \text{the square root of one over } (\mu_0 \epsilon_0)$ .

6. DOPPLER

Derive the Doppler Effect for light starting from the relativistic

## Physics 1C Fifth Sample Test

## 1. C DIVIDER

A LRC circuit has an input voltage of 120 volts.  $R=7,100$  ohms,  $L=7.7 \text{ E-6}$  Henries, and  $C=.00093$  Farads. What is the voltage across the capacitor for an input frequency of 7,900 HZ?

$$120/\text{PIX}(2*7,900)/.00093/\text{SQR}(7,100*7,100+(\text{PIX}(2*7,900)*7.7 \text{ E-6}-1/\text{PIX}(2*7,900)/.00093)**2)$$

A.  $9.43 \text{ E-6}$ , B.  $.000183$ , C.  $(.000366)$ , D.  $2.97 \text{ E9}$ , E.  $6.63 \text{ E9}$

## 2. FORM OF A TRAVELING WAVE

Show that  $E=E(x-vt)$  is a traveling wave and satisfies the wave equation:  $\text{del squared } E = (\mu \text{ zero})(\text{epslen zero}) \text{ second partial of } E / \text{second partial of } t$ .

## 3. E, B, AND C

Given that  $\text{del cross } E = - \text{partial } B / \text{partial } t$  and that  $E(x-ct)$ ,  $B=B(x-ct)$  show that E, B, and c are mutually perpendicular for electromagnetic waves.

## POYNTING'S VECTOR

Show that the power entering a resistor is given by  $i*i*R$  according to Poynting's vector.  $V=iR$ ,  $E=V/L$ ,  $\text{Integral}(B \text{ dl}) = \mu i$

## 5. WAVE GUIDE, SHORT

Show how to construct a wave that satisfies the boundary conditions of a wave guide and satisfies the wave equation:  $\text{Del squared } E = (1/c \text{ squared})(\text{second partial } E / \text{second partial } t)$ .